



# *LS, JK, and jj* Atomic Spectroscopic Terms and Spectroscopic Terms for small molecules



Roberto B. Faria

faria@iq.ufrj.br

[www.iq.ufrj.br/~faria](http://www.iq.ufrj.br/~faria)

*Instituto de Química*

*Universidade Federal do Rio de Janeiro*



## *JK coupling*

XXI Brazilian Meeting on Inorganic Chemistry, BMIC-2024

X Brazilian Meeting on Rare Earths, BMRE-2024

III Workshop on Theoretical Bioinorganic Chemistry, WTBC-2024

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# References

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- Cowan, R. D. *The theory of atomic structure and spectra*, University of California Press, 1981.

# *JK* coupling



# JK terms for carbon

The screenshot shows the NIST Atomic Spectra Database Levels Data page for C I. The top navigation bar includes links for ASD (selected), DATA (Lines, Levels), INFORMATION (List of Spectra, Ground States & Ionization Energies, Bibliography, Help). The main content area displays "C I 435 Levels Found" and "Z = 6, C isoelectronic sequence". A red box highlights the citation information: "Example of how to reference these results: Kramida, A., Raichenko, Yu., Reader, J., and NIST ASD Team (2021). *NIST Atomic Spectra Database* (ver. 5.9). [Online]. Available: <https://physics.nist.gov/asd> [2022, October 15]. National Institute of Standards and Technology, Gaithersburg, MD. DOI: <https://doi.org/10.18434/T4W30F>". Below this is a link to "BibTeX Citation (new window)". At the bottom, it says "Some data for neutral and singly-charged ions are available in the [Handbook of Basic Atomic Spectroscopic Data](#)". There are also links for "Primary data source" (Query NIST Bibliographic Database for C I), "Haris & Kramida 2017", and "Literature on C I Energy Levels".

**ASD** DATA ————— INFORMATION —————

LINES LEVELS List of SPECTRA GROUND STATES & IONIZATION ENERGIES Bibliography Help

**NIST Atomic Spectra Database Levels Data**

C I 435 Levels Found  
Z = 6, C isoelectronic sequence

Example of how to reference these results:  
Kramida, A., Raichenko, Yu., Reader, J., and NIST ASD Team (2021). *NIST Atomic Spectra Database* (ver. 5.9). [Online]. Available: <https://physics.nist.gov/asd> [2022, October 15]. National Institute of Standards and Technology, Gaithersburg, MD. DOI: <https://doi.org/10.18434/T4W30F>

[BibTeX Citation \(new window\)](#)

Some data for neutral and singly-charged ions are available in the [Handbook of Basic Atomic Spectroscopic Data](#)

Primary data source [Query NIST Bibliographic Database for C I \(new window\)](#)  
[Haris & Kramida 2017](#) [Literature on C I Energy Levels](#)

**NIST**  
National Institute of  
Standards and Technology  
Physical Meas. Laboratory

# JK terms for carbon

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Configuration	Term	J	g	Level (cm <sup>-1</sup> )
2s <sup>2</sup> 2p <sup>2</sup>	3P	0	1	0.0000000
		1	3	16.4167130
		2	5	43.4134567
2s <sup>2</sup> 2p <sup>2</sup>	1D	2	5	10 192.657
2s <sup>2</sup> 2p <sup>2</sup>	1S	0	1	21 648.030
2s2p <sup>3</sup>	5S°	2	5	33 735.121
2s <sup>2</sup> 2p3s	3P°	0	1	60 333.4476
		1	3	60 352.6584
		2	5	60 393.1693
2s <sup>2</sup> 2p3s	1P°	1	3	61 981.83211
2s2p <sup>3</sup>	3D°	3	7	64 086.96961
		1	3	64 089.8990
		2	5	64 090.99351

# JK terms for carbon

$2s^2 2p(^2P^{\circ}_{1/2}) 4f$	$^2[5/2]$	3 2	7 5	83 919.66322 83 919.77375
$2s^2 2p(^2P^{\circ}_{1/2}) 4f$	$^2[7/2]$	3 4	7 9	83 926.22434 83 926.42382
$2s^2 2p 4d$	$^1F^{\circ}$	3	7	83 947.2231
$2s^2 2p(^2P^{\circ}_{3/2}) 4f$	$^2[7/2]$	3 4	7 9	83 986.22212 83 986.4926
$2s^2 2p(^2P^{\circ}_{3/2}) 4f$	$^2[5/2]$	3 2	7 5	84 013.27526 84 013.4311
$2s^2 2p(^2P^{\circ}_{3/2}) 4f$	$^2[9/2]$	5 4	11 9	84 015.87795 84 016.2748
$2s^2 2p 4d$	$^1P^{\circ}$	1	3	84 032.1471
$2s^2 2p(^2P^{\circ}_{3/2}) 4f$	$^2[3/2]$	1 2	3 5	84 036.3320 84 036.4454

# LS coupling

$s^1$	$^2S_{1/2}$
$s^2$	$^1S_0$
$p^1, p^5$	$^2P_{3/2,1/2}^o$
$p^2, p^4$	$^3P_{2,1,0} \ ^1D_2 \ ^1S_0$
$p^3$	$^4S_{3/2}^o \ ^2D_{5/2,3/2}^o \ ^2P_{3/2,1/2}^o$
$p^6$	$^1S_0$
$d^1, d^9$	$^2D_{5/2,3/2}$
$d^2, d^8$	$^3F_{4,3,2} \ ^3P_{2,1,0} \ ^1G_4 \ ^1D_2 \ ^1S_0$
$d^3, d^7$	$^4F_{9/2,7/2,5/2,3/2} \ ^4P_{5/2,3/2,1/2} \ ^2H_{11/2,9/2} \ ^2G_{9/2,7/2} \ ^2F_{7/2,5/2} \ ^2D(2)_{5/2,3/2} \ ^2P_{3/2,1/2}$
$d^4, d^6$	$^5D_{4,3,2,1,0} \ ^3H_{6,5,4} \ ^3G_{5,4,3} \ ^3F(2)_{4,3,2} \ ^3D_{3,2,1} \ ^3P(2)_{2,1,0} \ ^1I_6 \ ^1G(2)_4 \ ^1F_3 \ ^1D(2)_2$ $^1S(2)_0$
$d^5$	$^6S_{5/2} \ ^4G_{11/2,9/2,7/2,5/2} \ ^4F_{9/2,7/2,5/2,3/2} \ ^4D_{7/2,5/2,3/2,1/2} \ ^4P_{5/2,3/2,1/2} \ ^2I_{13/2,11/2}$ $^2H_{11/2,9/2} \ ^2G(2)_{9/2,7/2} \ ^2F(2)_{7/2,5/2} \ ^2D(3)_{5/2,3/2} \ ^2P_{3/2,1/2} \ ^2S_{1/2}$
$d^{10}$	$^1S_0$

# LS coupling

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s <sup>1</sup>	<sup>2</sup> S <sub>1/2</sub>
s <sup>2</sup>	<sup>1</sup> S <sub>0</sub>
p <sup>1</sup> , p <sup>5</sup>	<sup>2</sup> P <sub>3/2,1/2</sub> <sup>o</sup>
p <sup>2</sup> , p <sup>4</sup>	<sup>3</sup> P <sub>2,1,0</sub> <sup>1</sup> D <sub>2</sub> <sup>1</sup> S <sub>0</sub>
p <sup>3</sup>	<sup>4</sup> S <sub>3/2</sub> <sup>o</sup> <sup>2</sup> D <sub>5/2,3/2</sub> <sup>o</sup> <sup>2</sup> P <sub>3/2,1/2</sub> <sup>o</sup>
p <sup>6</sup>	<sup>1</sup> S <sub>0</sub>
d <sup>1</sup> , d <sup>9</sup>	<sup>2</sup> D <sub>5/2,3/2</sub>
d <sup>2</sup> , d <sup>8</sup>	<sup>3</sup> F <sub>4,3,2</sub> <sup>3</sup> P <sub>2,1,0</sub> <sup>1</sup> G <sub>4</sub> <sup>1</sup> D <sub>2</sub> <sup>1</sup> S <sub>0</sub>
d <sup>3</sup> , d <sup>7</sup>	<sup>4</sup> F <sub>9/2,7/2,5/2,3/2</sub> <sup>4</sup> P <sub>5/2,3/2,2,1/2</sub> <sup>2</sup> H <sub>11/2,9/2</sub> <sup>2</sup> G <sub>9/2,7/2</sub> <sup>2</sup> F <sub>7/2,5/2</sub> <sup>2</sup> D(2) <sub>5/2,3/2</sub> <sup>2</sup> P <sub>3/2,1/2</sub>
d <sup>4</sup> , d <sup>6</sup>	<sup>5</sup> D <sub>4,3,2,1,0</sub> <sup>3</sup> H <sub>6,5,4</sub> <sup>3</sup> G <sub>5,4,3</sub> <sup>3</sup> F(2) <sub>4,3,2</sub> <sup>3</sup> D <sub>3,2,1</sub> <sup>3</sup> P(2) <sub>2,1,0</sub> <sup>1</sup> I <sub>6</sub> <sup>1</sup> G(2) <sub>4</sub> <sup>1</sup> F <sub>3</sub> <sup>1</sup> D(2) <sub>2</sub> <sup>1</sup> S(2) <sub>0</sub>
d <sup>5</sup>	<sup>6</sup> S <sub>5/2</sub> <sup>4</sup> G <sub>11/2,9/2,7/2,5/2</sub> <sup>4</sup> F <sub>9/2,7/2,5/2,3/2</sub> <sup>4</sup> D <sub>7/2,5/2,3/2,1/2</sub> <sup>4</sup> P <sub>5/2,3/2,1/2</sub> <sup>2</sup> I <sub>13/2,11/2</sub> <sup>2</sup> S <sub>5/2</sub> <sup>3</sup> G(2) <sub>4,3,2</sub> <sup>3</sup> F(2) <sub>3,2,1</sub> <sup>3</sup> D(2) <sub>2,1,0</sub> <sup>3</sup> P(2) <sub>2,1,0</sub> <sup>3</sup> D <sub>2,1,0</sub> <sup>3</sup> C <sub>2,1,0</sub>

# ***JK* terms for carbon**

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- Excited states involving one electron in orbitals f or g
- The core electrons interact by *LS* coupling
- The interaction with the excited electron is spin-independent.
- The *JK* scheme consider a new quantum number *K*.
- The *J* value is calculated by eq. (2), where *s* is the spin of the electron in the orbital f or g (*s* = 1/2)

$$K = J_{\text{core}} + \ell \quad (1)$$

$$J = K + s \quad (2)$$

# *JK* terms for carbon

---

$$2S+1 [K]_J$$

The spin multiplicity consider only the spin of the electron in the orbital f or g

$$2S+1 = 2(\frac{1}{2}) + 1 = 2$$

As a result, all terms are doublets

$$^2[K]_J$$

# *JK* terms for carbon

---

$$^2[K]_J$$

Electronic configuration:  $2s^2 2p^1 4f^1$

Core configuration  $2s^2 2p^1$  terms:  ${}^2P_{3/2,1/2}^\circ$

Let us choose the term  ${}^2P_{1/2}^\circ$  ( $J_{\text{core}} = \frac{1}{2}$ )

$$2s^2 2p^1 ({}^2P_{1/2}^\circ) 4f^1$$

$$K = J_{\text{core}} + \ell, J_{\text{core}} + \ell - 1, J_{\text{core}} + \ell - 2, |J_{\text{core}} - \ell| \quad (1)$$

	0	1	2	3	4	5	6	7	8	9	10	11 ...
$\ell$ (for electrons)	s	p	d	f	g	h	i	k	l	m	n	o ...

# *JK* terms for carbon

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$$^2[K]_J$$

$$^2P_{1/2}^\circ \ (J_{\text{core}} = 1/2)$$

$$2s^2 \ 2p^1 \ (^2P_{1/2}^\circ) \ 4f^l$$

$$K = J_{\text{core}} + \ell, J_{\text{core}} + \ell - 1, J_{\text{core}} + \ell - 2, |J_{\text{core}} - \ell| \quad (1)$$

$$K = 1/2 + 3, |1/2 - 3| = 7/2, 5/2$$

	0	1	2	3	4	5	6	7	8	9	10	11	...
$\ell$ (for electrons)	s	p	d	f	g	h	i	k	l	m	n	o	...

# *JK* terms for carbon

---

$$^2[K]_J$$



$$^2[7/2]_J \quad ^2[5/2]_J$$

# *JK* terms for carbon

---

$$^2[K]_J$$



$$^2[7/2]_J \quad ^2[5/2]_J$$

Using eq. (2) to calculate the  $J$  values.

$$J = K + s, K + s - 1, K + s - 2 \dots |K - s| \quad (2)$$

$$s = 1/2$$

# ***JK* terms for carbon**

---

$$^2[K]_J$$



For the term  $^2[7/2]_J$

$$J = K + s, K + s - 1, K + s - 2 \dots |K - s| \quad (2)$$

$$J = 7/2 + 1/2, 7/2 - 1/2, = 4, 3$$

# *JK* terms for carbon

---

$$^2[K]_J$$



Resulting in terms  $^2[7/2]_{4,3}$

# ***JK* terms for carbon**

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$$^2[K]_J$$



For the term  $^2[5/2]_J$

$$J = K + s, K + s - 1, K + s - 2 \dots |K - s| \quad (2)$$

$$s = 1/2$$

$$J = 5/2 + 1/2, 5/2 - 1/2, = 3, 2$$

# *JK* terms for carbon

---

$$^2[K]_J$$



Resulting in terms  $^2[5/2]_{3,2}$

# *JK* terms for carbon

---

$$^2[K]_J$$



Collecting the terms

$$^2[7/2]_{4,3} \quad ^2[5/2]_{3,2}$$

# JK terms for carbon

$2s^2 2p^1 (^2P_{1/2}^\circ) 4f^1$

$^2[5/2]_{3,2}$

$^2[7/2]_{4,3}$

$2s^2 2p(^2P_{1/2}^\circ) 4f$	$^2[5/2]$	3 2	7 5	83 919.66322 83 919.77375
$2s^2 2p(^2P_{1/2}^\circ) 4f$	$^2[7/2]$	3 4	7 9	83 926.22434 83 926.42382
$2s^2 2p4d$	$^1F^\circ$	3	7	83 947.2231
$2s^2 2p(^2P_{3/2}^\circ) 4f$	$^2[7/2]$	3 4	7 9	83 986.22212 83 986.4926
$2s^2 2p(^2P_{3/2}^\circ) 4f$	$^2[5/2]$	3 2	7 5	84 013.27526 84 013.4311
$2s^2 2p(^2P_{3/2}^\circ) 4f$	$^2[9/2]$	5 4	11 9	84 015.87795 84 016.2748
$2s^2 2p4d$	$^1P^\circ$	1	3	84 032.1471
$2s^2 2p(^2P_{3/2}^\circ) 4f$	$^2[3/2]$	1 2	3 5	84 036.3320 84 036.4454

# *JK* terms for carbon

---

$$^2[K]_J$$

Electronic configuration:  $2s^2 2p^1 4f^1$

Core configuration  $2s^2 2p^1$  terms:  ${}^2P_{3/2,1/2}^\circ$

Let us choose the term  ${}^2P_{3/2}^\circ$  ( $J_{\text{core}} = 3/2$ )

$$2s^2 2p^1 ({}^2P_{3/2}^\circ) 4f^1$$

$$K = J_{\text{core}} + \ell, J_{\text{core}} + \ell - 1, J_{\text{core}} + \ell - 2, |J_{\text{core}} - \ell| \quad (1)$$

	0	1	2	3	4	5	6	7	8	9	10	11 ...
$\ell$ (for electrons)	s	p	d	f	g	h	i	k	l	m	n	o ...

# *JK* terms for carbon

---

$$^2[K]_J$$

$$^2P_{3/2}^\circ \ (J_{\text{core}} = 3/2)$$

$$2s^2 \ 2p^1 \ (^2P_{3/2}^\circ) \ 4f^l$$

$$K = J_{\text{core}} + \ell, J_{\text{core}} + \ell - 1, J_{\text{core}} + \ell - 2, |J_{\text{core}} - \ell| \quad (1)$$

$$K = 3/2 + 3, \dots |3/2 - 3| = 9/2, 7/2, 5/2, 3/2$$

	0	1	2	3	4	5	6	7	8	9	10	11	...
$\ell$ (for electrons)	s	p	d	f	g	h	i	k	l	m	n	o	...

# *JK* terms for carbon

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$^2[K]_J$

$2s^2\ 2p^1\ (^2P_{3/2}^\circ)\ 4f^l$

$^2[9/2]_J \quad ^2[7/2]_J \quad ^2[5/2]_J \quad ^2[3/2]_J$

# *JK* terms for carbon

---

$$^2[K]_J$$



$$^2[9/2]_J \quad ^2[7/2]_J \quad ^2[5/2]_J \quad ^2[3/2]_J$$

$$J = K + s, K + s - 1, K + s - 2 \dots |K - s| \quad (2)$$

$$s = 1/2$$

# *JK* terms for carbon

---

$$^2[K]_J$$



For the term  $^2[9/2]_J$

$$J = K + s, K + s - 1, K + s - 2 \dots |K - s| \quad (2)$$

$$s = 1/2$$

$$J = 9/2 + 1/2, 9/2 - 1/2, = 5, 4$$

# *JK* terms for carbon

---

$$^2[K]_J$$



Resulting in terms  $^2[9/2]_{5,4}$

# ***JK* terms for carbon**

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$$^2[K]_J$$



For the term  $^2[7/2]_J$

$$J = K + s, K + s - 1, K + s - 2 \dots |K - s| \quad (2)$$

$$s = 1/2$$

$$J = 7/2 + 1/2, 7/2 - 1/2, = 4, 3$$

# *JK* terms for carbon

---

$$^2[K]_J$$



Resulting in terms  $^2[7/2]_{4,3}$

# *JK* terms for carbon

---

$$^2[K]_J$$



Using a similar procedure

$$^2[9/2]_{5,4} \ ^2[7/2]_{4,3} \ ^2[5/2]_{3,2} \ ^2[3/2]_{2,1}$$

# JK terms for carbon

$2s^2 2p^1 (^2P_{3/2}^\circ) 4f^1$

$^2[9/2]_{5,4}$

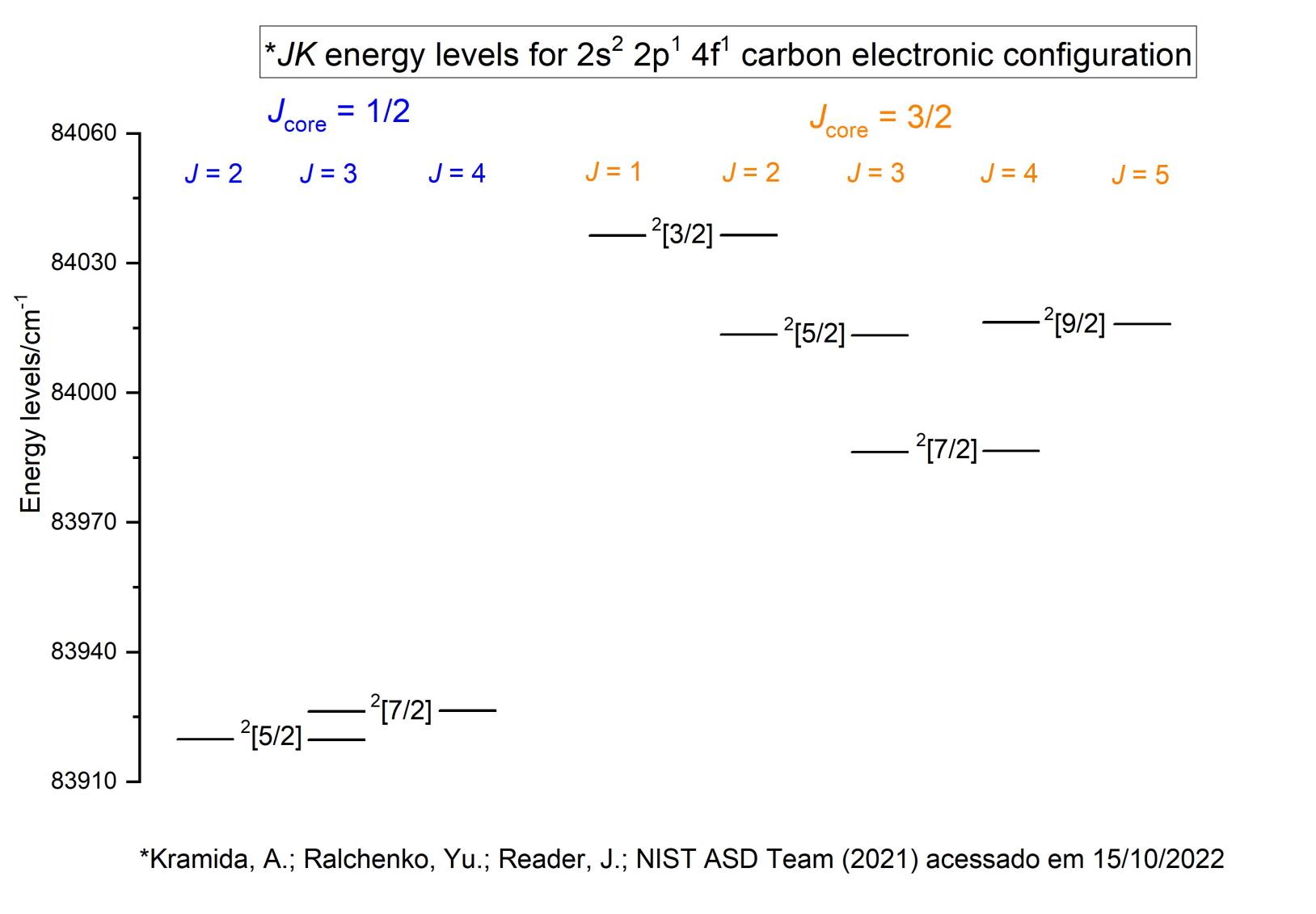
$^2[7/2]_{4,3}$

$^2[5/2]_{3,2}$

$^2[3/2]_{2,1}$

	$2s^2 2p(^2P_{1/2}) 4f$	$^2[5/2]$	3 2	7 5	83 919.66322 83 919.77375
	$2s^2 2p(^2P_{1/2}) 4f$	$^2[7/2]$	3 4	7 9	83 926.22434 83 926.42382
	$2s^2 2p 4d$	$^1F^\circ$	3	7	83 947.2231
	$2s^2 2p(^2P_{3/2}) 4f$	$^2[7/2]$	3 4	7 9	83 986.22212 83 986.4926
	$2s^2 2p(^2P_{3/2}) 4f$	$^2[5/2]$	3 2	7 5	84 013.27526 84 013.4311
	$2s^2 2p(^2P_{3/2}) 4f$	$^2[9/2]$	5 4	11 9	84 015.87795 84 016.2748
	$2s^2 2p 4d$	$^1P^\circ$	1	3	84 032.1471
	$2s^2 2p(^2P_{3/2}) 4f$	$^2[3/2]$	1 2	3 5	84 036.3320 84 036.4454

# JK terms for carbon



**THE END**

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